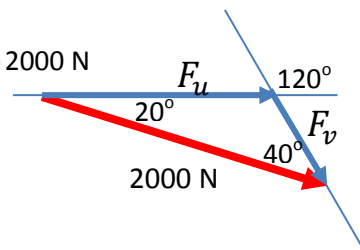
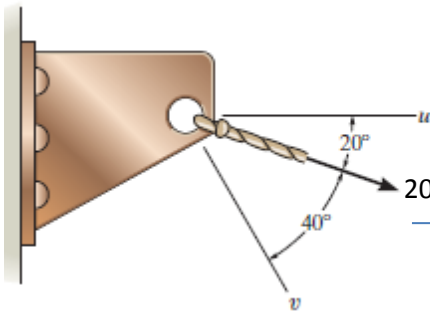


Final Exam

Answer the following questions.

Question 1: (6 points)

Resolve the 2000 N force shown Figure into components acting along the u and v axes and determine the magnitudes of these components.

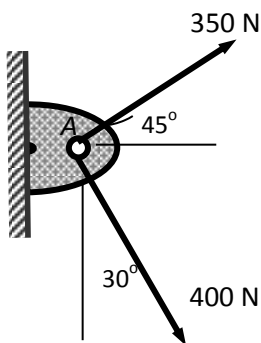


$$\frac{F_u}{\sin 40} = \frac{2000}{\sin 120} \rightarrow F_u = 1484.5 \text{ N}$$

$$\frac{F_v}{\sin 20} = \frac{2000}{\sin 120} \rightarrow F_v = 790 \text{ N}$$

Question 2: (6 points):

Determine the magnitude and direction of the two forces shown in Figure.



$$\rightarrow \sum F_x = 350 \cos 45 + 400 \sin 30 = 447.5 \text{ N}$$

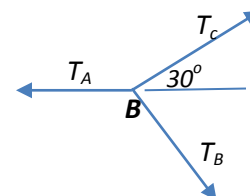
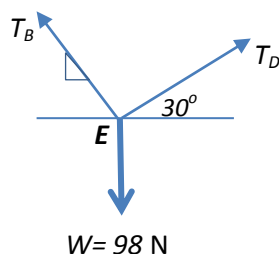
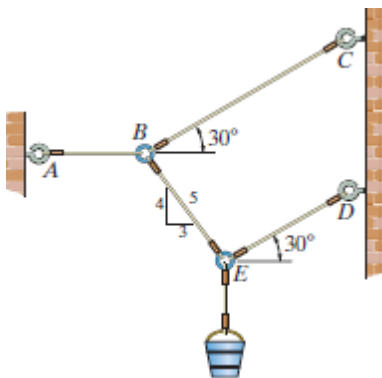
$$\uparrow \sum F_y = 350 \sin 45 - 400 \cos 30 = -90 \text{ N}$$

$$R = \sqrt{(\sum F_x)^2 + (\sum F_y)^2} = 456.5 \text{ N}$$

$$\theta = \tan^{-1} \left(\frac{\sum F_y}{\sum F_x} \right) = \tan^{-1} \left(\frac{-90}{447.5} \right) = -11.4^\circ$$

Question 3: (10 points)

The 10-kg bucket is supported at E by a system of five cords as shown. Determine the force in each cord for equilibrium.



Equilibrium of point E:

$$\sum F_x = 0; T_D \cos 30 = \frac{3}{5} T_B \rightarrow T_D = 0.693 T_B$$

$$\sum F_y = 0; T_D \sin 30 + \frac{4}{5} T_B = 98 \rightarrow 1.147 T_B = 98$$

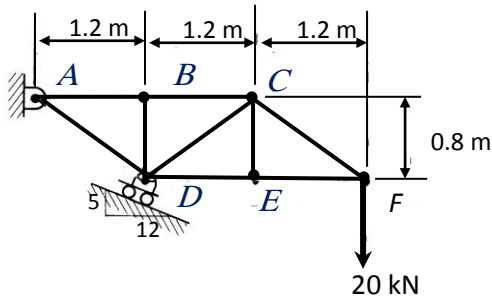
$$\therefore T_B = 85.5 \text{ N} \text{ and } \therefore T_D = 59.2 \text{ N} \text{ Ans}$$

Equilibrium of point B:

$$\sum F_x = 0; T_C \cos 30 + \frac{3}{5} T_B = T_A$$

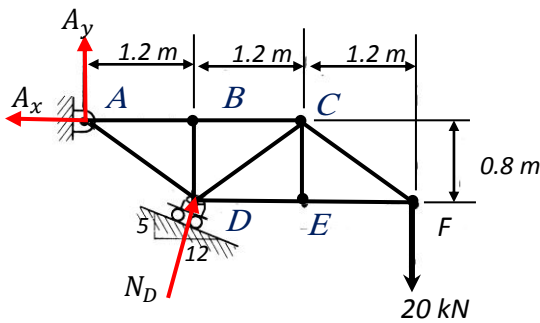
$$\sum F_y = 0; T_C \sin 30 = \frac{4}{5} T_B \rightarrow T_C = 136.8 \text{ N Ans}$$

$$\therefore T_A = 169.8 \text{ N} \text{ Ans.}$$



Question 4: (8 points)

The frame shown in figure is supported by a pin at A and roller at D . The frame is subjected to 20 kN load at F . Determine the reactions at A and B .



$$\sum M_A = 0; \quad N_D \cos\theta(1.2) + N_D \sin\theta(0.8) = 20(3.6)$$

$$(1.108 + 0.308)N_D = 72 \quad \rightarrow N_D = 50.8 \text{ kN}$$

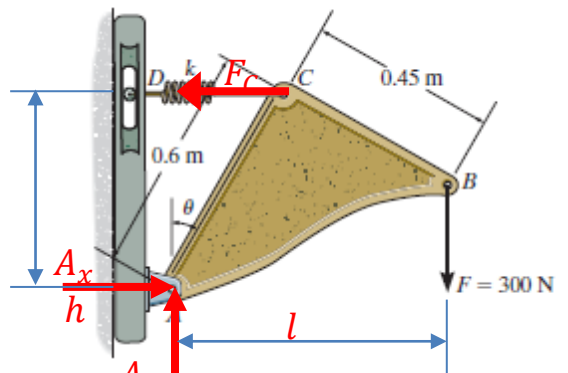
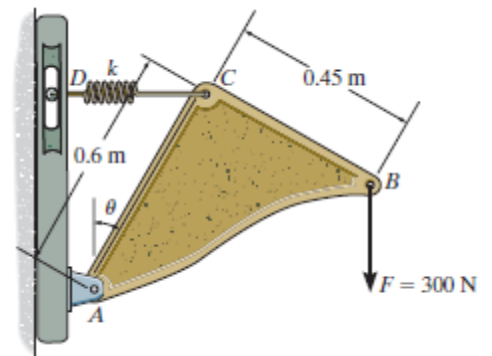
$$\sum F_x = 0; \quad A_x = N_D \sin\theta = 50.8\left(\frac{5}{13}\right) = 19.53 \text{ kN}$$

$$\sum F_y = 0; \quad A_y + N_D \cos\theta = 20$$

$$A_y = 20 - 50.8\left(\frac{12}{13}\right) = -26.89 \text{ kN}$$

Question 5: (8 points)

Spring CD remains in the horizontal position at all times due to the roller at D . If $\theta = 30^\circ$, Determine the force developed in the spring at C and the vertical and horizontal components of the reaction at hinge A .



$$\sum M_A = 0; \quad F_C \times h = F \times l$$

$$\therefore F_C = 300(0.69)/0.52 \quad \rightarrow F_C = 398.4 \text{ N}$$

$$\sum F_x = 0; \quad A_x = F_C = 398.4 \text{ N}$$

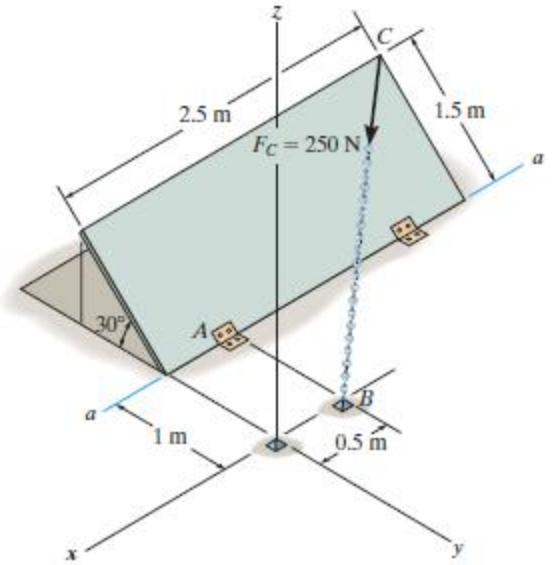
$$\sum F_y = 0; \quad A_y = F = 300 \text{ N}$$

$$l = 0.6 \sin 30 + 0.45 \cos 30 = 0.69$$

$$h = 0.6 \cos 30 = 0.52$$

Question 6: (7 points)

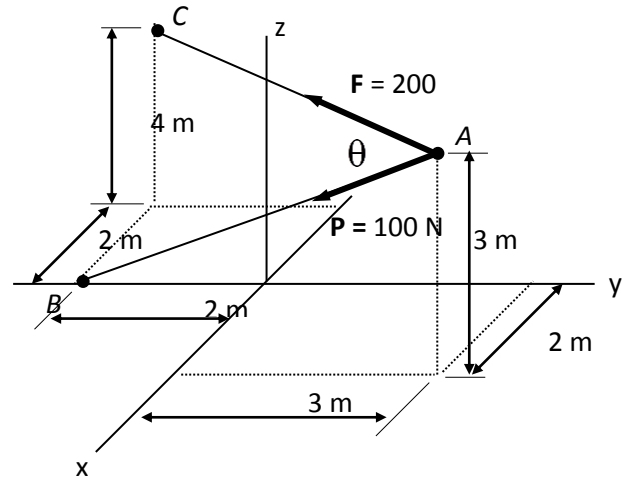
The force F_c shown in Figure is expressed in Cartesian form as: $F_c = (160 i + 183 j - 60 k)N$. Determine the moment of this force about point A.



$$M_A = r_{AB} \times F = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 1 & 0 \\ 160 & 183 & -60 \end{vmatrix} = -60 \mathbf{i} - 160 \mathbf{k}$$

Question 7: (7 points)

Determine the angle θ between the tails of the two forces shown.



$C: (-2, -2, 4)$; $B: (0, -2, 0)$; $A: (2, 3, 3)$

$$\mathbf{r}_{AB} = -2 \mathbf{i} - 5 \mathbf{j} - 3 \mathbf{k}$$

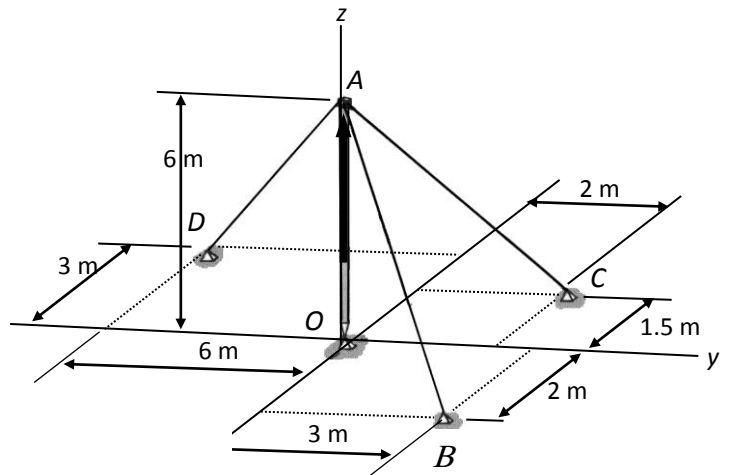
$$\mathbf{r}_{AC} = -4 \mathbf{i} - 5 \mathbf{j} - \mathbf{k}$$

$$\cos \theta = \frac{\mathbf{r}_{AB} \cdot \mathbf{r}_{AC}}{(\mathbf{r}_{AB})(\mathbf{r}_{AC})} = \frac{8+25+3}{(6.164)(6.481)} = 0.901$$

$$\theta = \cos^{-1}(0.901) = 25.69^\circ$$

Question 8: (8 points)

The mast OA is supported by three cables. If cable AB is subjected to a tension of 500 N, and cable AC is subjected to a tension of 300 N and cable AD is subjected to a tension of 200 N determine the resultant of the three forces.



$C: (-1.5, 2, 0)$; $B: (2, 3, 0)$; $D: (-3, -6, 0)$; $A: (0, 0, 6)$

$$\mathbf{r}_{AB} = 2 \mathbf{i} + 3 \mathbf{j} - 6 \mathbf{k}; \quad r_{AB} = 7$$

$$\mathbf{r}_{AC} = -1.5 \mathbf{i} + 2 \mathbf{j} - 6 \mathbf{k}; \quad r_{AC} = 6.5$$

$$\mathbf{r}_{AD} = -3 \mathbf{i} - 6 \mathbf{j} - 6 \mathbf{k}; \quad r_{AD} = 9$$

$$\mathbf{F}_{AB} = \frac{500}{7}(2 \mathbf{i} + 3 \mathbf{j} - 6 \mathbf{k}) = 142.86 \mathbf{i} + 214.29 \mathbf{j} - 428.57 \mathbf{k}$$

$$\mathbf{F}_{AC} = \frac{300}{6.5}(-1.5 \mathbf{i} + 2 \mathbf{j} - 6 \mathbf{k}) = -69.23 \mathbf{i} + 92.31 \mathbf{j} - 276.92 \mathbf{k}$$

$$\mathbf{F}_{AD} = \frac{200}{9}(-3 \mathbf{i} - 6 \mathbf{j} - 6 \mathbf{k}) = -66.67 \mathbf{i} - 133.33 \mathbf{j} - 133.33 \mathbf{k}$$

$$\therefore \mathbf{R} = 6.96 \mathbf{i} + 173.27 \mathbf{j} - 838.82 \mathbf{k}$$